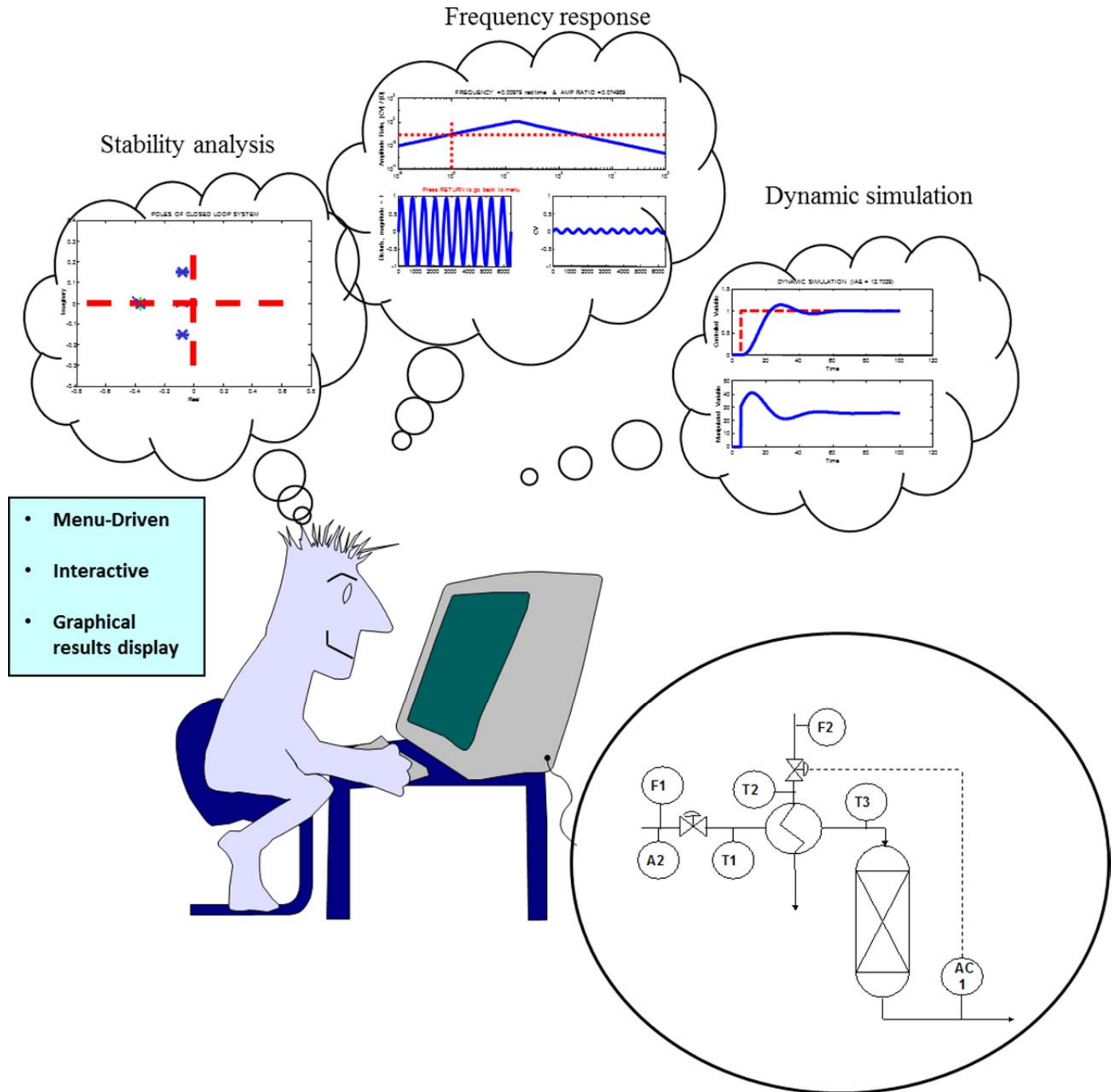


THE SOFTWARE LABORATORY

S_LOOP:

Single-loop Feedback Control System Analysis



Version 4.0 for MATLAB and Octave
Copyright © 1995, 2003, 2011 by T. Marlin

S_LOOP: SINGLE-LOOP FEEDBACK CONTROL SYSTEM ANALYSIS

by Michelle Gretzinger, Daniel Zyngier and Thomas Marlin

INTRODUCTION

One of the challenges to the engineer learning process control is relating theoretical concepts to the time-domain behavior of dynamic systems. This **menu-driven, interactive** software package provides learning experiences for single-variable feedback systems, including stability analysis, frequency response, and time-domain dynamic performance. Many of the solved examples in the textbook can be repeated and extended using this software.

The basic design of the software enables the user to use simple menus to enter parameters, select specific calculations and display results. **No programming is required.** To provide a simple yet flexible system, the process dynamics are represented by a general transfer function model, fourth order with lead and dead time, and the controller is limited to a proportional-integral-derivative (PID) feedback algorithm. The user can tailor this system by setting selected parameters to zero.

SYSTEM STRUCTURE

The overall structure of the system is given in Figure 1, and the main Main Menu is shown in Figure 2. The Main Menu appears when the program is first executed and remains the principle interface throughout the session. In a typical session, the user first defines the process and controller through Submenus 1-3; then, he/she selects calculations through the remaining submenus. An important feature is the use of the *same models* for all calculations, so that the user can clearly relate the frequency response analysis to time-domain behavior.

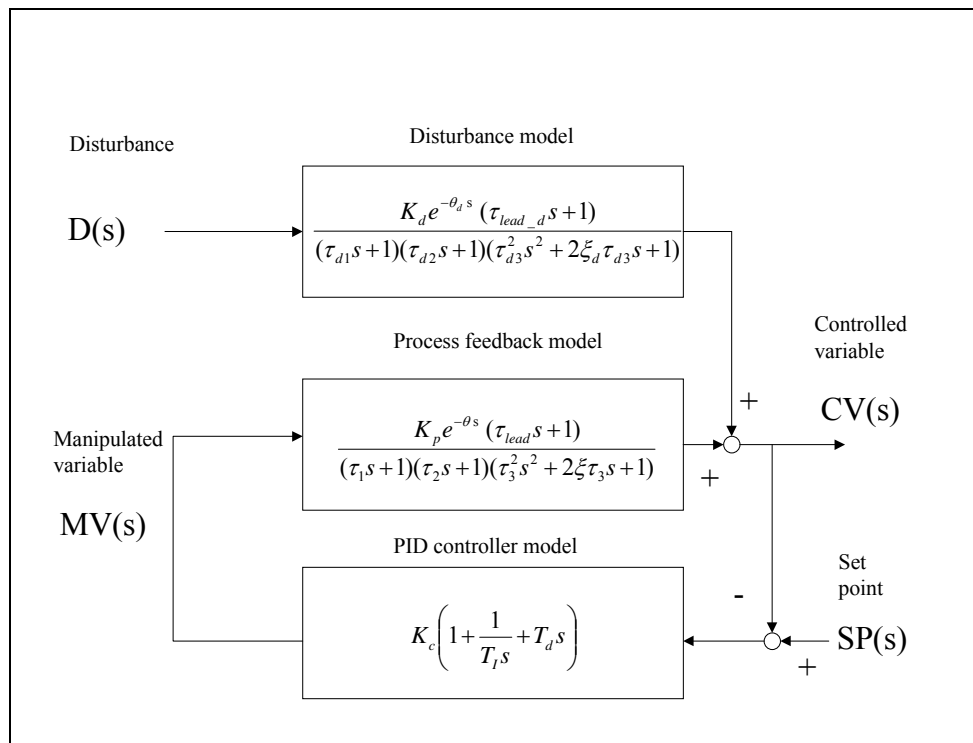


Figure 1. Block diagram of the dynamic system in S_LOOP.

```

*****
*           S_LOOP:   SINGLE LOOP CONTROL SYSTEM ANALYSIS           *
*                                                                 *
*           McMASTER UNIVERSITY CHEMICAL ENGINEERING               *
*           =====                                               *
*                               Version 4.0                           *
*                                                                 *
*                               MAIN MENU                             *
*                                                                 *
*****
SELECT THE APPROPRIATE MENU ITEM
1) Modify Feedback Process Model Parameters
2) Modify Disturbance Process Model Parameters
3) Modify PID Controller Tuning Constants
4) Plot Poles of Closed Loop System
5) Bode Plot for GOL for Stability Analysis
6) Bode Plot for Process, Gp
7) Bode Plot for Closed Loop Responses
8) Dynamic Simulation of System
0) Quit to Matlab
Please enter the desired selection:

```

Figure 2. Main Menu for the S_LOOP software.

PROCESS AND CONTROLLER DATA

The user enters the process and controller parameters in the first three Submenus.

Submenu

- 1) **Process Model** - The process model, $G_p(s)$, parameters are entered using Submenu 1. Recall that the process model defines the dynamics between the manipulated variable and the controlled variable. Any parameter can be set to zero without causing numerical errors. Note that user can also define noise, which is used only for the measurement of the controlled variable in the time-domain simulation.
- 2) **Disturbance Model** - The disturbance model, $G_d(s)$, parameters are entered through Submenu 2. Recall that the disturbance model defines the dynamics between the disturbance and the controlled variable. Any parameter can be set to zero without causing numerical errors.
- 3) **Submenu 3: PID Controller** - The control algorithm is *Old Faithful*, the proportional-integral-derivative or PID controller. This is by far the most widely used controller in industry. It has three adjustable tuning parameters, which are defined in Submenu 3: the gain (K_c), the integral time (T_I), and the derivative time (T_d). The user can turn off the controller by setting $K_c = 0$. If the user sets the integral time to zero, the integral mode is removed from the algorithm (a divide by zero does not occur).

The user can select a PID controller implemented as a continuous controller (really digital executed every step in the dynamic simulation) or a digital controller (executed at the period defined by the user).

ANALYSIS AND SIMULATION

The remaining Submenus enable the user to select from the following analysis calculations for the process and control system previously defined through Submenus 1-3.

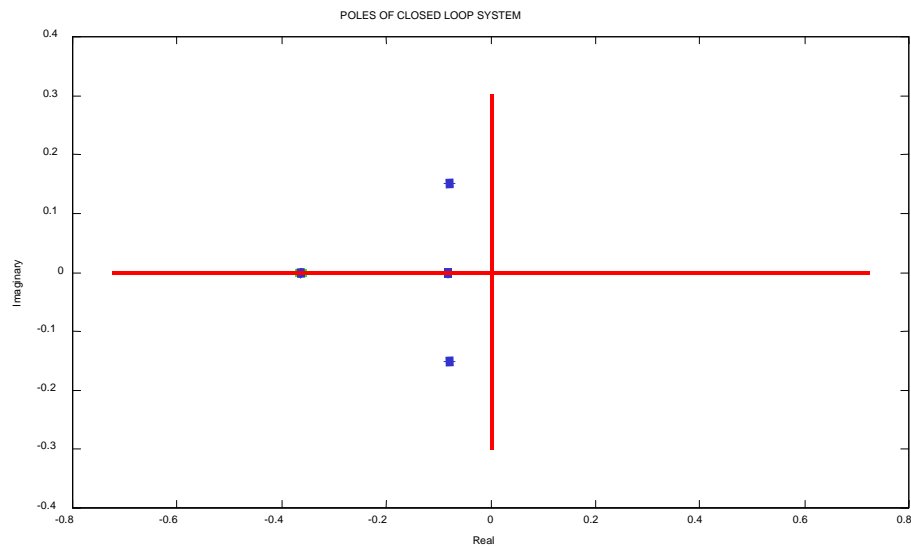
The following frequency response analyses can be computed without the user having to perform calculations involving complex numbers. The emphasis is on understanding concepts, not hand calculations

Submenu

- 4) **Poles** - Solve for and plot the roots of the characteristic equation (i.e., the poles) of the closed-loop system to evaluate stability. The program calculates the poles, plots them, and prints the pole values.

This can only be done if the characteristic equation is a polynomial in “s” and does not contain a dead time. If a dead time occurs in the feedback process model, a message is provided to the user explaining that the calculations cannot be performed.

This analysis is performed for the system defined through menus 1 and 3. If the PID controller gain is set to zero, the closed-loop analysis becomes an open-loop analysis of the process model.



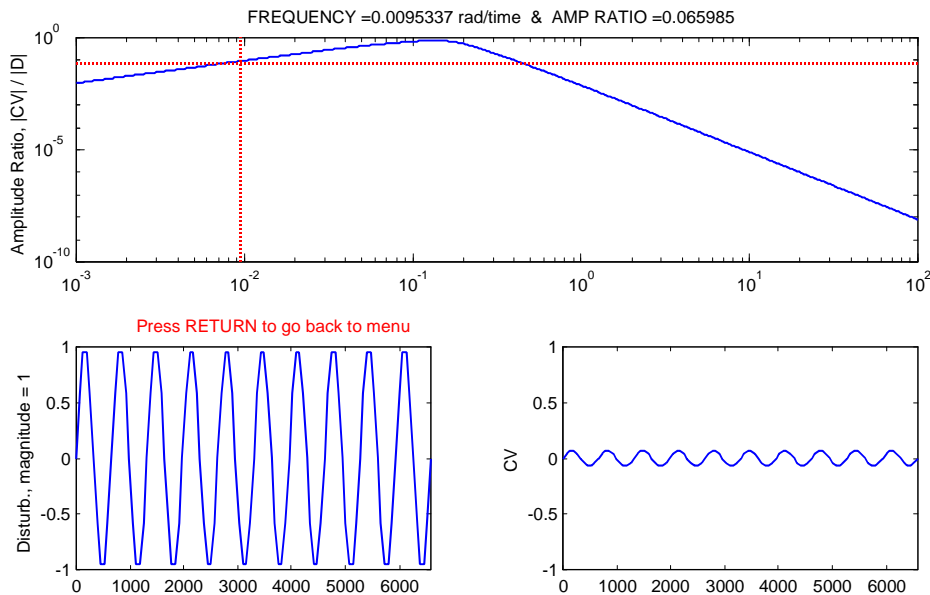
The poles are:
-0.3626
-0.0778 + 0.1504i
-0.0778 - 0.1504i
-0.0818

- 5) **Bode Stability** - Calculate the frequency response displayed as a Bode plot of $G_{OL}(j\omega) = G_p(\omega)G_v(\omega)G_c(\omega)G_s(\omega)$. The program provides a plot and the values for the frequency and amplitude ratio at the first crossing of -180 degrees within the frequency defined by the user.

With the controller defined with a P-only with a gain of 1.0 ($K_c = 1$, $T_I = 0$, and $T_d = 0$), this plot can be used for tuning using the Ziegler-Nichols method.

With the PID controller tuned to any values thought appropriate, this plot can be used to determine

- 7) **Closed-loop Frequency Response** - Calculate the amplitude ratio of the closed-loop control system to evaluate the control performance over the frequency range defined by the user. The user can select the input to be either a disturbance or set point. Also, you can plot the sine input and output at any frequency. (The sine plot at the point picked by the user is available in MATLAB, but not Octave.)



- 8) **Dynamic Simulation** - Calculate the closed-loop dynamic response in the time-domain to a step input, which is introduced as a step at 5% of the total simulation time. If the combination of the total time and time step, Δt , yields a large number of steps, the simulation would be unnecessarily time consuming. Therefore, the program checks these inputs automatically and ensures that the number of steps is less than the maximum allowed. If the program resets the time step, the software displays a message to the user and changes the value displayed in the menu.

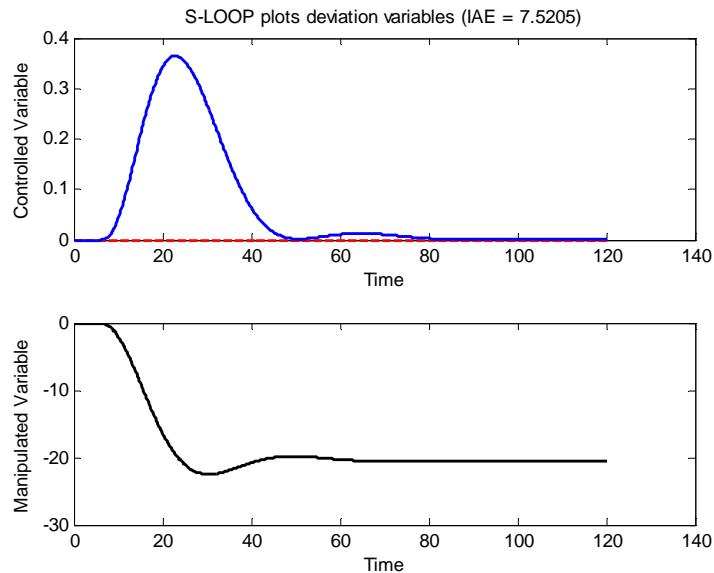
The user can select the size of the desired input step, and set all others to zero. The type of input can be one of the following.

- a) process reaction curve (step in the manipulated variable with the controller off),
- b) disturbance, or
- c) set point change.

The controller can be selected to be a continuous PID (executed every simulation time step) or a digital PID (executed at the period selected by the user).

The variables are plotted in deviation variables from their initial values of 0.0. The manipulated variable does not observe any bound, although all final elements have limits in a real plant.

The control performance metric IAE of the controlled variable is reported in the figure, except for transient where the step is made in the manipulated variable for a process reaction curve experiment.



```

*****
* S_LOOP: SINGLE LOOP CONTROL SYSTEM DYNAMIC SIMULATION *
*
*   Hints:  1) All inputs are steps at 5% of total time *
*           2) If Entry 5 is non-zero, PID controller *
*              is turned off *
*           3) Select Time step (delta t) to approximate *
*              a) for the smallest time constant, *
*                 (delta t) / tau = 0.05 *
*              b) dead time/ (delta t) = integer *
*           4) Usually, (total time) / (time step) < 1000 *
*           5) Digital controller exec time integer of *
*              simulation delta time *
*****
SELECT THE APPROPRIATE MENU ITEM

                                PRESENT VALUES
1) Total simulation time          120.00
2) Time step for simulation       0.200

3) Set point change              0.00
4) Disturbance change            0.80
5) Process reaction curve MV input 0.00

6) Select continuous/digital controller, currently continuous
   (Controller executed every simulation time step)

7) Execute dynamic simulation
8) Return to main menu
Enter the desired selection:

```

SAMPLE SESSION

After entering MATLAB, the user must define the MATLAB path where the s_loop m-files are stored; naturally, the path will be different for every installation. After the correct directory has been defined, the user types s_loop and strikes enter in the MATLAB window to begin the program. The Main Menu will appear on the screen, indicating that the S_LOOP program is running.

For this sample session, entries for Example 9.2 from the textbook are discussed. The essential data are summarized in the following.

$$\frac{CV(s)}{MV(s)} = G_p(s) = \frac{K_p}{(\tau_p s + 1)^3} = \frac{0.039}{(5s + 1)^3}$$

$$\frac{CV(s)}{D(s)} = G_d(s) = \frac{K_d}{(\tau_d s + 1)^3} = \frac{1}{(5s + 1)^3}$$

First, the user must enter the data from the attached table into the program. This is done for the process parameters (Submenu 1), the disturbance (Submenu 2), and the controller (Submenu 3).

Note that program returns to the Main Menu simply by striking the "enter" with a blank entry from any Submenu.

Submenu

- 1) The process model defined in Submenu 1 includes all process and instrumentation elements in the feedback loop. The tacit assumption is that the single model between the manipulated and controlled variables includes the process and final element, i.e., $G_p(s)=G'_p(s)G_v(s)$, and that the sensor contributes negligible dynamics, i.e., $G_s(s)=1.0$. The third order mixing system can be represented in the S_LOOP format using the following

$$\begin{aligned} \frac{0.039}{(5s + 1)^3} &= \frac{0.039}{(5s + 1)(5s + 1)^2} = \frac{0.039}{(5s + 1)(25s^2 + 10s + 1)} \\ &= \frac{K_p}{(\tau_1 s + 1)(\tau_2 s + 1)(\tau_3^2 s^2 + 2\tau_3 \xi s + 1)} \end{aligned}$$

Thus, $K_p = 0.039$, $\tau_{lead} = 0$, $\tau_1 = 0$, $\tau_2 = 5$, $\tau_3 = 5$ and $\xi = 1.0$. We will enter $K_n = 0$ to remove noise from the dynamic simulation.

- 2) The disturbance model is entered via Submenu 2. In this case, only the steady-state gain is different from the process model, although in other cases many parameters may be different.

Thus, $K_d = 1.0$, $\tau_{lead_d} = 0$, $\tau_{d1} = 0$, $\tau_{d2} = 5$, $\tau_{d3} = 5$ and $\xi_d = 1.0$.

- 3) The controller tuning is of $K_c = 30$, $T_i = 11$ and $T_d = 0.80$ is entered through Submenu 3. At any time the user wishes to turn off the controller, the controller gain can be set to zero ($K_c = 0$).

- 8) The purpose of the exercise is to evaluate the dynamic response; thus, Submenu 8 is selected. The user may select the total time, here 200 to be consistent with Figure 9.6. The time step is selected to give good accuracy without exceeding the maximum steps; thus, 0.20 is selected. This gives $\Delta t/\tau = 0.04$, which should provide reasonable accuracy. Note that for systems with dead time, which this example does not have, the dead time is approximated as an *integer multiple* of the step size.

Continuing in Submenu 8, the user has the option of a unit step in the set point, disturbance, or manipulated variable (a process reaction curve). The user selects the desired input by entering a non-zero value for the changing input and zero values for the other inputs. If the user enters a non-zero value for the manipulated variable, the feedback controller is automatically turned off.

The PID controller is selected to be “continuous”.

The simulation is started by selecting Submenu item 7. The results are automatically plotted on the screen and can be compared with the answers in Example 9.2 and Figure 9.6.

Although Example 9.2 does not deal with other aspects of the system behavior, they are discussed here to demonstrate all program features.

Submenu

- 4) The roots of the characteristic equation are the exponents of the time-domain solution for the dynamics. For this system, the characteristic equation is

$$0 = 1 + G_p(s)G_c(s) = 1 + \frac{.039}{(1 + 5s)^3} 30 \left(1 + \frac{1}{11s} + 0.8s \right)$$

First, the program rearranges this equation into a polynomial form; the user *does not* have to perform this reformulation. The roots for this equation are

$$-0.3626, \quad -0.0778 + 0.1504i, \quad -0.0778 - 0.1504i, \quad \text{and } -0.0818.$$

Since all real parts are negative, the system is (bounded input-output) stable. Also, since two roots are complex the system is underdamped, as can be seen in the dynamic response.

If the controller gain is set to zero, the roots of the **process** transfer function, $G_p(s)$, are evaluated.

- 5) The Bode plot of the transfer function including all elements in the feedback path, $G_{OL}(s)$, is evaluated via this Submenu. Recall that this transfer function can be used to i) evaluate the tuning by Zeigler-Nichols method by setting $G_c(s)=1.0$ ($K_c=1.0$, $T_i=0$, and $T_d=0$) or 2) testing the stability of the system by checking the amplitude ratio at the critical frequency with any controller, $G_c(s)$.

Since the controller tuning has been entered, $G_{OL}(s)$ is given in the following.

$$G_{OL}(s) = G_p(s)G_c(s) = \frac{.039}{(1 + 5s)^3} 30 \left(1 + \frac{1}{11s} + 0.80s \right)$$

For the parameters in the example, the Bode plot demonstrates that $|G_{OL}(j\omega_c)| < 1.0$ at the critical frequency, i.e., the frequency at which the phase angle equals -180° . The program provides the user with values of the critical frequency (0.35 rad/min) and amplitude ratio (0.139) in the MATLAB window. Therefore, the system is stable.

- 6) The Bode plot of the process, $G_p(j\omega)$, is evaluated. This can be used in determining how the process without control would affect a sine disturbance.
- 7) The closed-loop Bode diagram is evaluated in this Submenu. Recall that this frequency response gives the amplitude of the controlled variable relative to the input for a range of frequencies. The user must enter the choice of set point or disturbance input to obtain the appropriate result.

$$\text{setpoint : } \frac{CV(s)}{SP(s)} = \frac{G_p(s)G_c(s)}{1 + G_p(s)G_c(s)} = \frac{\frac{.039}{(1 + 5s)^3} 30 \left(1 + \frac{1}{11s} + 0.80s \right)}{1 + \frac{.039}{(1 + 5s)^3} 30 \left(1 + \frac{1}{11s} + 0.80s \right)}$$

$$\text{disturbance : } \frac{CV(s)}{D(s)} = \frac{G_d(s)}{1 + G_p(s)G_c(s)} = \frac{\frac{1}{(1 + 5s)^3}}{1 + \frac{.039}{(1 + 5s)^3} 30 \left(1 + \frac{1}{11s} + 0.80s \right)}$$

The disturbance is selected through the Submenu item 3 defining parameter “d”, and the result is plotted in a Bode plot. The result for the disturbance shows that $|CV(j\omega)|/|D(j\omega)|$ has

- a small magnitude (small error) at low frequencies (because of effective feedback control),
- a small magnitude (small error) at high frequencies (because of the process filtering the disturbance)
- a resonance peak at a frequency of about 1 rad/min where feedback control is not very effective.

The user can evaluate the set point Bode plot by selecting the “s” input and running the program again. The Bode plot shows the excellent set point tracking at low frequencies and poor tracking at high frequencies.

The value of the program is that the user can evaluate control performance and stability using various frequency- domain and time-domain methods, and s/he may then compare the results and change process and controller parameters to evaluate the effects.

LIMITATIONS

S_LOOP should provide excellent experience with frequency-dependent and time-domain behavior of single-loop feedback control. The major limitations are noted below.

- 1) The number of time steps, determined from (total time)/(step size), is not allowed to be greater than a maximum limit. This limit is currently set at 20000 time steps. Typically, the time duration (t_{end}) divided by the step size (Δt) less than 1000 provides adequate accuracy for dynamic systems in the textbook.

The dead time used in the dynamic simulations of the time-domain dynamic response (but not the frequency response calculations) are rounded to an *integer multiple* of the simulation step size.

The controller execution period is rounded to an *integer multiple* of the simulation time step.

- 2) The calculation of the frequency response involves the phase angle that may exceed -180° . The program uses the MATLAB feature (UNWRAP function) which *usually* correctly recognizes a change of quadrant and accounts for this fact in calculating the arctangent; however, this feature is not foolproof. Spurious results, phase angles larger than their proper values, can be obtained; therefore, the Bode plot should be scrutinized when performing the Bode stability analysis. Narrowing the range of the frequencies often corrects the problem, should it occur.
- 3) The process and disturbance transfer functions are limited to fourth order. No higher orders can be simulated.

VERIFYING TEXTBOOK RESULTS

A good starting point is to compare the time-domain and frequency/stability results for many of the examples and confirm that both methods give consistent results and provide complementary insights into dynamic behavior. To assist the student, the S_LOOP parameters for most single-loop textbook Examples are provided in the following tables, and additional hints are provided after the tables.

Table 1. Parameters for Examples in Textbook Chapter 4, 7, 8, and 9

| Case | process model | | | | | | | disturbance | | controller | | | disturbance | simulation | |
|-----------------------------|---------------|----------|--------------|----------|----------|----------|-------|-------------|----------------|------------|-------|-------|-------------|------------|-----------|
| | K_p | θ | $\tau_{i,d}$ | τ_1 | τ_2 | τ_3 | ξ | K_d | input | K_c | T_i | T_d | s/d | Δt | t_{end} |
| Example 4.15 | 1.0 | 0 | 0 | 7.9 | 0 | 0 | 1 | --- | --- | --- | --- | --- | | --- | --- |
| Example 4.16 | 0.448 | 0 | 0 | 8.25 | 8.25 | 0 | 1 | --- | --- | --- | --- | --- | | --- | --- |
| Example 7.3 Figure 7.10a | .039 | 0 | 0 | 0 | 5 | 5 | 1 | 1.0 | $\Delta D= 1$ | 40 | 11 | 0 | | .25 | 200 |
| Figure 7.10b | .039 | 0 | 0 | 0 | 5 | 5 | 1 | 1 | $\Delta D= 1$ | 9 | 11 | 0 | | .25 | 200 |
| Figure 8.3 | .039 | 0 | 0 | 0 | 5 | 5 | 1 | 1.0 | $\Delta D=0.8$ | 0-220 | 0 | 0 | | .1 | 200 |
| Example 8.5 Figure 8.9 | -33.9 | 0 | 0 | 11.9 | 0 | 0 | --- | --- | --- | -.059 | 0.95 | 0 | | 0.1 | 50 |
| Figure 9.2 | 1 | 5 | 0 | 0 | 5 | 0 | --- | 1 | $\Delta D= 1$ | 1.14 | 10 | 0 | | 1 | 200 |
| | 1 | 5 | 0 | 0 | 5 | 0 | --- | 1 | $\Delta D= 1$ | 0.62 | 10 | 0 | | 1 | 200 |
| | 1 | 5 | 0 | 0 | 5 | 0 | --- | 1 | $\Delta D= 1$ | 1.52 | 10 | 0 | | 1 | 200 |
| | 1 | 5 | 0 | 0 | 5 | 0 | --- | 1 | $\Delta D= 1$ | 0.89 | 7 | 0 | | 1 | 200 |
| | 1 | 5 | 0 | 0 | 5 | 0 | --- | 1 | $\Delta D= 1$ | 1.04 | 5.3 | 2.1 | | 1 | 200 |
| | 1 | 5 | 0 | 0 | 5 | 0 | --- | 1 | $\Delta D= 1$ | 0.88 | 6.4 | 0.82 | | 1 | 200 |
| Example 9.1 | 1 | 2 | 0 | 8 | 0 | 0 | --- | 1 | --- | 3.0 | 3.7 | 1.1 | | 1 | 100 |
| Example 9.2 | .039 | 0 | 0 | 0 | 5 | 5 | 1 | 1.0 | $\Delta D=0.8$ | 30 | 11 | 0.88 | | .25 | 200 |
| Example 9.3 | .039 | 0 | 0 | 0 | 5 | 5 | 1 | 1.0 | $\Delta D=0.8$ | 30 | 11 | 0.88 | | .25 | 200 |
| Example 9.5 Figure 9.11a | 2 | 2 | 0 | 0 | 8 | 0 | --- | 1.0 | $\Delta D= 2$ | 0.9 | 5.2 | 0 | | .12 | 100 |
| Figure 9.11b | 2 | 3 | 0 | 0 | 7 | 0 | --- | 1.0 | $\Delta D= 2$ | 0.9 | 5.2 | 0 | | .12 | 100 |
| Figure 9.11c | 2 | 2 | 0 | 0 | 8 | 0 | --- | 1.0 | $\Delta D= 2$ | 1.5 | 6.0 | 0 | | .12 | 100 |
| Figure 9-11d | 2 | 3 | 0 | 0 | 7 | 0 | --- | 1.0 | $\Delta D= 2$ | 1.5 | 6.0 | 0 | | .12 | 100 |
| Figure 9.12 | .05 | 10 | 0 | 0 | 10 | 0 | --- | --- | $\Delta SP=1$ | 12 | 10 | 0 | | .25 | 200 |
| Figure 9.13 | .05 | 10 | 0 | 0 | 10 | 0 | --- | --- | $\Delta SP=1$ | 5 | 10 | 0 | | .25 | 200 |
| Figure 9.14 | .05 | 10 | 0 | 0 | 10 | 0 | --- | --- | $\Delta SP=1$ | 12 | 5 | 0 | | .25 | 200 |

Table 2. Parameters for Examples in Textbook Chapter 10

| Case | process model | | | | | | | disturbance | | controller | | | disturbance | simulation | |
|--------------------------------|---------------|----------|-------------|----------|----------|----------|-------|-------------|----------------|------------|-------|-------|-------------|------------|-----------|
| | K_p | θ | τ_{1d} | τ_1 | τ_2 | τ_3 | ξ | K_d | input | K_c | T_I | T_d | s/d | Δt | t_{end} |
| Example 10.4 | 0.1 | 0 | 0 | 0.50 | 0.50 | 0 | --- | --- | --- | 15 | 1 | 0 | | | |
| Example 10.5 | .039 | 0 | 0 | 0 | 5 | 5 | 1 | --- | --- | 0-220 | 0 | 0 | | | |
| Example 10.6 | .039 | 0 | 0 | 0 | 5 | 0 | --- | --- | --- | 1 | 0 | 0 | | | |
| Example 10.7 | .039 | 0 | 0 | 0 | 5 | .091 | 1.56 | --- | --- | 1-6000 | 0 | 0 | | | |
| Example 10.8 | .1 | 1 | 0 | .5 | .5 | 0 | --- | --- | --- | 15 | 1 | 0 | | | |
| Example 10.9 | .039 | 0 | 0 | 0 | 0 | 5 | 1 | --- | --- | --- | --- | --- | | | |
| Example 10.10 | .039 | 0 | 0 | 0 | 5 | 5 | 1 | 1.0 | $\Delta D=0.8$ | 94.5 | 14.9 | 0 | | .25 | 200 |
| Example 10.11 | .1 | 1 | 0 | .5 | .5 | 0 | --- | --- | --- | 1.0 | 0.0 | 0 | | | |
| Example 10.12 (n=3) | 1 | 0 | 0 | 0 | 5 | 5 | 1 | --- | --- | 1 | 0 | 0 | | | |
| Example 10.13 (A) | 1 | 2 | 0 | 0 | 8 | 0 | --- | --- | --- | 1 | 0 | 0 | | | |
| Example 10.13 (B) | 1 | 8 | 0 | 0 | 2 | 0 | --- | --- | --- | 1 | 0 | 0 | | | |
| Example 10.14 | .039 | 0 | 0 | 0 | 5 | 5 | 1 | --- | --- | 122 | 0 | 0 | | | |
| | .039 | 0 | 0 | 0 | 5 | 5 | 1 | --- | --- | 122 | 8 | 0 | | | |
| Example 10.15 nominal | 1 | 1 | 0 | 9 | 0 | 0 | --- | --- | --- | 1 | 0 | 0 | | | |
| Example 10.15 process I | 1 | .5 | 0 | 9.5 | 0 | 0 | --- | --- | --- | 6.8 | 3.2 | 0 | | | |
| Example 10.15 process II | 1 | 2 | 0 | 8 | 0 | 0 | --- | --- | --- | 6.8 | 3.2 | 0 | | | |
| Example 10.16 | .039 | 0 | 0 | 0 | 5 | 5 | 1 | 1.0 | $\Delta D=1$ | 206 | 0 | 0 | | .05 | 100 |
| Example 10.17 | .039 | 0 | 0 | 0 | 5 | 5 | 1 | 1.0 | $\Delta D=1$ | 94.5 | 14.9 | 0 | | .12 | 200 |
| Example 10.18 3-tank | .039 | 0 | 0 | 0 | 5 | 5 | 1 | --- | --- | 1 | 0 | 0 | | | |
| Example 10.18 approx. model | .039 | 5.5 | 0 | 0 | 10.5 | 0 | 1 | --- | --- | 1 | 0 | 0 | | | |

Table 3. Parameters for Examples in Textbook Chapter 13

| Case | process model | | | | | | | disturbance | | controller | | | disturbance selection | simulation | |
|--|---------------|----------|--------------|----------|----------|----------|-------|-------------|---------------------|------------|-------|-------|-----------------------|------------|-----------|
| | K_p | θ | $\tau_{i,d}$ | τ_i | τ_2 | τ_3 | ξ | K_d | input | K_c | T_i | T_d | s/d | Δt | t_{end} |
| Figure 13.3 | 1 | 15 | 0 | 0 | 30 | 0 | --- | .48 | | 0.6 | 30 | 0 | d | | |
| Example 13.1A Figure 13.5 | 1 | 1 | 0 | 0 | 1 | 0 | --- | 1 | | 0.85 | 1.5 | 0 | d | | |
| Example 13.1B | 1 | 4 | 0 | 0 | 4 | 0 | --- | 1 | | 0.85 | 6.0 | 0 | d | | |
| Example 13.1C | 1 | .5 | 0 | 0 | 1.5 | 0 | --- | 1 | | 1.70 | 1.3 | 0 | d | | |
| Example 13.1D | 0.1 | .5 | 0 | 0 | 1.5 | 0 | --- | 1 | | 17.0 | 1.3 | 0 | d | | |
| Example 13.2 | 1 | 1 | 0 | 0 | 2 | 0 | --- | 1 | | 1 | 2 | 0 | d | | |
| Example 13.3 | 1 | 0.5 | 0 | 0 | 1.5 | 0 | --- | 1 | | 1.70 | 1.3 | 0 | s | | |
| Example 13.8 (linear approximation) | -1.66 | 0 | -8.0 | 8.25 | 8.25 | 0 | --- | --- | $\Delta SP = -.014$ | -0.45 | 13 | 0 | | 0.12 | 100 |
| Figure 13.16a | .039 | 0 | 0 | 0 | 5 | 5 | 1 | 1 | --- | 30 | 11 | 0 | d | | |
| Figure 13.16b | .039 | 5.5 | 0 | 0 | 10.5 | 0 | --- | 1 | | 30 | 11 | 0 | d | | |

Hints for Selected Textbook Examples

Chapter 7

Example 7.1 This process model cannot be simulated in S_LOOP because it is higher than fourth order.

Example 7.2 The third order mixing system can be represented in the S_LOOP format as shown in the following

$$\begin{aligned} \frac{K}{(5s + 1)^3} &= \frac{K}{(5s + 1)(5s + 1)^2} = \frac{K}{(5s + 1)(25s^2 + 10s + 1)} \\ &= \frac{K}{(\tau_1 s + 1)(\tau_2 s + 1)(\tau_3^2 s^2 + 2\tau_3 \xi s + 1)} \end{aligned}$$

Thus, $\tau_{lead}=0$, $\tau_1=0$, $\tau_2=5$, $\tau_3=5$ and $\xi=1.0$.

Chapter 8

Figure 8.3 The stability of these systems can be determined using Submenu 4 to calculate the roots of the characteristic equation.

Figure 8.5 It is *not possible* to reproduce these responses because the controller equation must be modified to eliminate the proportional while retaining the integral.

Example 8.5 The closed-loop transfer function is second order, and the characteristic equation has the roots $-0.126 \pm 0.40j$. The negative real part indicates that the linear system is stable, and the large complex part indicates oscillatory behavior in the time domain.

Chapter 9

Figure 9.2 The time step is given a value of 1.0 to be consistent with the tuning optimization studies in Appendix D. This gives $\Delta t/(\theta+\tau)=0.10$ which is a bit high but within reason.

Table 9.2 See comment above.

Example 9.1 See comment above. It is *not possible* to optimize with S_LOOP; thus, only the simulation is performed.

Example 9.4 This cannot be calculated by S_LOOP because the non-linear equations representing the process were used, see workbook Exercises 11.2 and 11.3.

Chapter 10

Example 10.7 This third order system can be approximated by the general fourth order process model by recognizing that the two fast systems, the sensor and valve, can be combined to give

$$\frac{0.039 K_c}{5s+1} \frac{1}{(0.25s+1)(0.33s+1)} = \frac{0.039 K_c}{5s+1} \frac{1}{.00825s^2 + 0.283s + 1}$$

$$= \frac{0.039 K_c}{\tau_2 s + 1} \frac{1}{\tau_3^2 + 2\tau_3 \xi s + 1}$$

Therefore, $\tau_{lead}=0$, $\tau_1=0$, $\tau_2=5$, $\tau_3=0.0908$ and $\xi=1.56$.

Ex. 10.12 Only the cases with $n=1$ and $n=3$ can be calculated with the limited process model structure in S_LOOP.

Ex. 10.14 The stability of the closed-loop system can also be determined by calculating the roots of the characteristic equation.

Chapter 11

Care must be exercised when using S_LOOP to investigate the effects of changing the controller execution period, since the simulation time step and the controller execution period are the same in S_LOOP. Generally, S_LOOP should be used for continuous systems using a small time step size.

Chapter 12

It is not possible to repeat the studies on filtering because S_LOOP has no option to add noise to the measurement signal. The general effect on the controlled variable performance can be investigated by adding a filter to the system, which in S_LOOP can be easily done by adding an additional time constant to the feedback process dynamics. Note that this "filter" influences the plotted variables, so that the CV after being filtered would appear in the results plot.

Chapter 13

Example 13.8 The results of this simulation using S_LOOP are approximate since the flow of solvent is changing during the transient and influencing the dynamics significantly. Figure 13.15 was determined by numerically solving the non-linear model of the system.

Note that S_LOOP assumes the numerator lead term has the form $(\tau_{ld}s+1)$, with the lead time allowed to be positive or negative.

Figure 13.14 Sample results in Figures 13.13a&b can be obtained by simulating a first order with dead time process with PI control using the Ciancone tuning and $\Delta t/(\theta+\tau)=0.10$.

Example 13.9 The calculation of the manipulated variable frequency response cannot be performed with S_LOOP because it does not have an option for the transfer function in equation (13.19).

Ex. 13.10 This calculation cannot be performed with S_LOOP because S_LOOP is limited to a fourth order system.